# Combining Inductive and Analytical Learning

[Read Ch. 12] [Suggested exercises: 12.1, 12.2, 12.6, 12.7, 12.8]

- Why combine inductive and analytical learning?
- KBANN: Prior knowledge to initialize the hypothesis
- TangetProp, EBNN: Prior knowledge alters search objective
- FOCL: Prior knowledge alters search operators

## Inductive and Analytical Learning

### Inductive learning

Hypothesis fits data Statistical inference Requires little prior knowledge Learns from scarce data Syntactic inductive bias

### Analytical learning

Hypothesis fits domain the Deductive inference Bias is domain theory

### What We Would Like

Inductive learning

Analytical learning

Plentiful data No prior knowledge Perfect prior knowledge Scarce data

## General purpose learning method:

- No domain theory  $\rightarrow$  learn as well as inductive methods
- ullet Perfect domain theory  $\to$  learn as well as Prolog-EBG
- Accomodate arbitrary and unknown errors in domain theory
- Accomodate arbitrary and unknown errors in training data

### Domain theory:

 $\begin{aligned} \text{Cup} \leftarrow \text{Stable}, \text{Liftable}, \text{OpenVessel} \\ \text{Stable} \leftarrow \text{BottomIsFlat} \\ \text{Liftable} \leftarrow \text{Graspable}, \text{Light} \\ \text{Graspable} \leftarrow \text{HasHandle} \\ \text{OpenVessel} \leftarrow \text{HasConcavity}, \text{ConcavityPointsUp} \end{aligned}$ 

## Training examples:

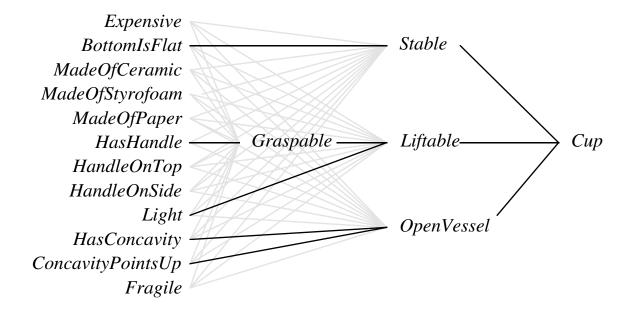
	Cups			Non-Cups						
BottomIsFlat										
ConcavityPoints Up										
Expensive										
Fragile										
HandleOnTop										
HandleOnSide										
HasConcavity									$\sqrt{}$	
HasHandle										
Light										
MadeOfCeramic										
MadeOfPaper										
MadeOfStyrofoam										$\sqrt{}$

## **KBANN**

## KBANN (data D, domain theory B)

- 1. Create a feedforward network h equivalent to B
- 2. Use Backprop to tune h to fit D

# Neural Net Equivalent to Domain Theory



# Creating Network Equivalent to Domain Theory

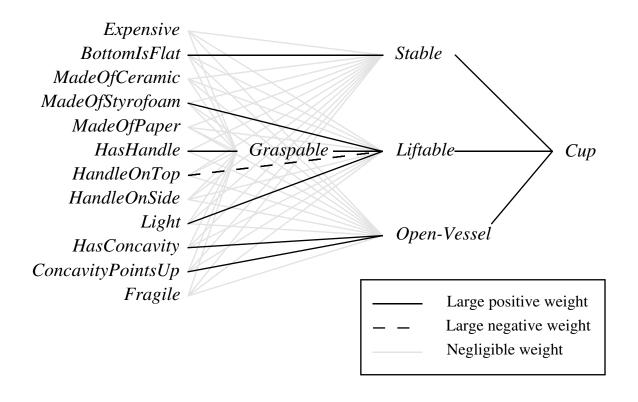
Create one unit per horn clause rule (i.e., an AND unit)

- Connect unit inputs to corresponding clause antecedents
- For each non-negated antecedent, corresponding input weight  $w \leftarrow W$ , where W is some constant
- For each negated antecedent, input weight  $w \leftarrow -W$
- Threshold weight  $w_0 \leftarrow -(n-.5)W$ , where n is number of non-negated antecedents

Finally, add many additional connections with near-zero weights

$$Liftable \leftarrow Graspable, \neg Heavy$$

# Result of refining the network



## KBANN Results

Classifying promoter regions in DNA leave one out testing:

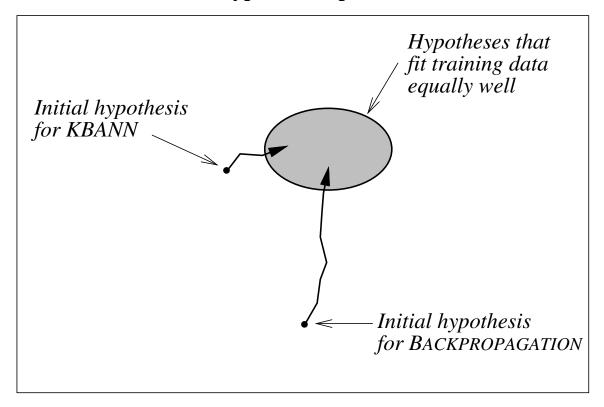
• Backpropagation: error rate 8/106

• KBANN: 4/106

Similar improvements on other classification, control tasks.

# Hypothesis space search in KBANN

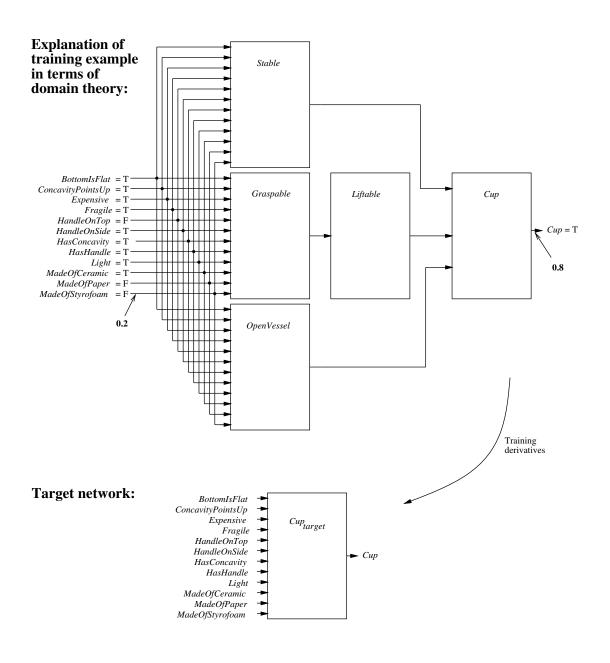
#### **Hypothesis Space**



## **EBNN**

#### Key idea:

- Previously learned approximate domain theory
- Domain theory represented by collection of neural networks
- Learn target function as another neural network



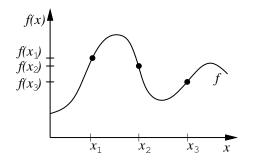
## Modified Objective for Gradient Descent

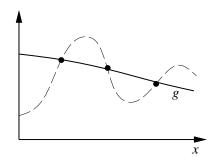
$$E = \sum_{i} \left[ (f(x_i) - \hat{f}(x_i))^2 + \mu_i \sum_{j} \left( \frac{\partial A(x)}{\partial x^j} - \frac{\partial \hat{f}(x)}{\partial x^j} \right)_{(x=x_i)}^2 \right]$$

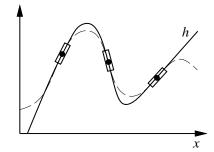
where

$$\mu_i \equiv 1 - \frac{|A(x_i) - f(x_i)|}{c}$$

- f(x) is target function
- $\hat{f}(x)$  is neural net approximation to f(x)
- A(x) is domain theory approximation to f(x)

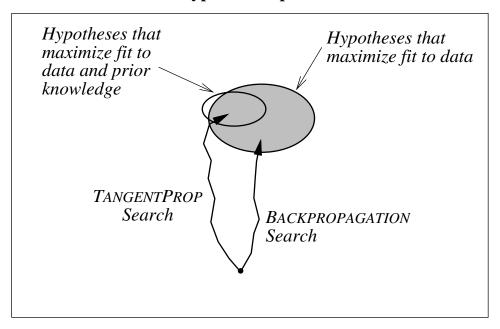




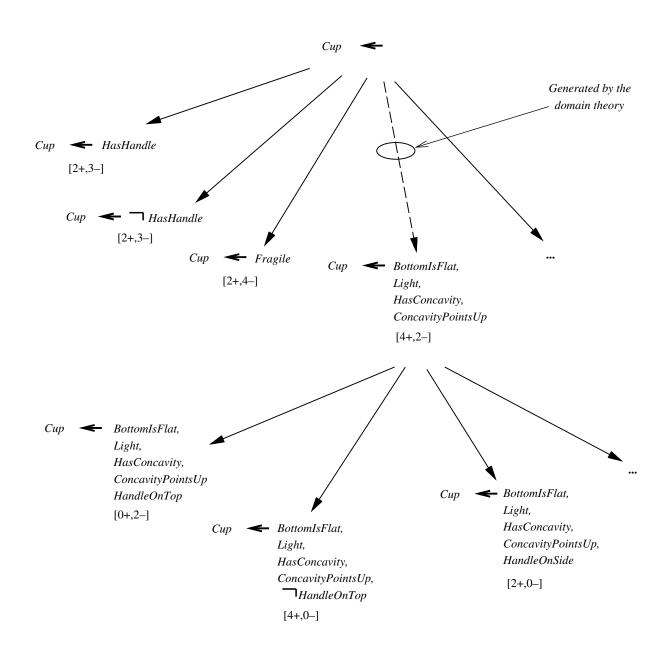


# Hypothesis Space Search in EBNN

#### **Hypothesis Space**



## Search in FOCL



### FOCL Results

Recognizing legal chess endgame positions:

- 30 positive, 30 negative examples
- FOIL: 86%
- FOCL: 94% (using domain theory with 76% accuracy)

NYNEX telephone network diagnosis

- 500 training examples
- FOIL: 90%
- FOCL: 98% (using domain theory with 95% accuracy)